A macromolecule in a solvent: Adaptive resolution molecular dynamics simulation

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The authors report adaptive resolution molecular dynamics simulations of a flexible linear polymer in solution. The solvent, i.e., a liquid of tetrahedral molecules, is represented within a certain radius from the polymer’s center of mass with a high level of detail, while a lower coarse-grained resolution is used for the more distant solvent. The high resolution sphere moves with the polymer and freely exchanges molecules with the low resolution region through a transition regime. The solvent molecules change their resolution and number of degrees of freedom on the fly. The authors show that their approach correctly reproduces the static and dynamic properties of the polymer chain and surrounding solvent. © 2007 American Institute of Physics. [DOI: 10.1063/1.2714540]

I. INTRODUCTION

The structural properties of polymers, i.e., long chain molecules of either synthetic or biological origin, in solution are crucial for many technical and biological processes and properties. Depending on the chemical nature of the chains, they can be solvated in a polar (e.g., water) or nonpolar (e.g., oil) solvent, where the details strongly depend on temperature, salt content, etc. In general the structure of polymers in solution is determined by the local solvent molecule-polymer bead interaction. In the case of a polymer in a solvent, one typically distinguishes three regions of solvent quality: good, Θ or marginal, and poor. In the case of a good solvent the solvent-solvent, solvent-polymer, and polymer-polymer interactions effectively result in a situation where the chain monomers repel each other (excluded volume effect). As a result the chains are extended in their overall conformation and the average size \( \langle R^2(N) \rangle \) scales as \( \langle R^2 \rangle \approx N^{2x} \) with \( N \) being the number of monomers and \( x \) being a universal critical exponent with \( x = 0.6 \) in three dimensions. For poor solvent we observe just the opposite and the chains collapse into a dense globule, \( \langle R^2 \rangle \approx N^{2/3} \). In the Θ regime the effects of the mutual excluded volume of the beads and the mutual effective attraction due to the presence of the solvent just cancel. As a consequence to a first approximation the chains adopt a random walk conformation, i.e., \( \langle R^2 \rangle \approx N \). In the limit of \( N \to \infty \) the Θ point is a tricritical point. For charged polymers, such as polyelectrolytes the situation is more complicated and will not be discussed here. As long as the solvent does not induce special local correlations beyond a rather unspecific attraction/repulsion and as long as one is not studying dynamical properties, polymer solutions are usually studied with an implicit solvent. There the solvent is omitted completely and the complicated local interactions are accounted for by an effective interaction potential between the chain beads. Studies of that kind have a long tradition in polymer science and lead to the establishment of a rather complete picture of the overall phase diagram. Beyond that there are, however, many situations where it becomes difficult or even questionable to ignore the local structure of the solvent. The solvent can play an important role for the functional properties of macromolecules. For example, dehydration studies of proteins solvated in water demonstrated that at least a monolayer of water is needed for full protein functionality. On the other hand, a very important issue of macromolecule solvation is its influence on the structure and dynamics of the surrounding solvent. Therefore, a detailed study of interactions of a macromolecule with a solvent beyond effective coupling parameters is quite often required for an understanding of the macromolecule’s structure, dynamics, and function. To determine the interactions of a solvent with a macromolecular solute chemistry specific interactions on the atomic level of detail have to be considered. However, the resulting solvating phenomena manifest themselves at mesoscopic and macroscopic scales and thus the overall structure of the chains. Due to large number of atoms and the corresponding degrees of freedom (DOFs) such systems are difficult to tackle using all-atom computer simulations. Moreover, the vast majority of the simulation time typically is spent treating the solvent and not the polymer or protein. A step to bridge the gap between the time and length scales accessible to simulations at an atomistic level of detail and solvating phenomena on longer/larger time and length scales is given by hybrid multiscale schemes that concurrently couple different physical descriptions of the system (see, e.g., Refs. 6–13).

Recently, we have proposed an adaptive resolution molecular dynamics (MD) scheme (AdResS) that concurrently couples the atomistic and mesoscopic length scales of a generic solvent. In a first application we studied a liquid of tetrahedral molecules where an atomistic region was separated from the mesoscopic one by a flat or a spherical boundary. The two regimes with different resolutions freely exchanged molecules while maintaining the thermodynamical equilibrium in the system. The spatial regions of different...
resolutions remained constant during the course of the simulations. More recently this approach was extended to the study of water.\textsuperscript{17} In the present paper, we generalize our approach to the study of a polymer chain in solution. The chain is surrounded by solvent with “atomistic” resolution. When the chain moves around, the sphere of atomistically resolved solvent molecules moves together with the center of mass of the chain. By this the chain is free to move around, although the explicit resolution sphere is much smaller than the overall simulation volume. This enables us to efficiently treat solvation phenomena, because only the solvent in the vicinity of a macromolecule is always represented with a sufficiently high level of detail so that the specific interactions between a solvent and a solute are correctly taken into account. The solvent farther away from the polymer, where the high resolution is no longer required, is represented on a more coarse-grained level. In this work, a macromolecule is represented by a generic flexible polymer chain\textsuperscript{18} embedded in a solvent of tetrahedral molecules introduced in Refs.\textsuperscript{14} and \textsuperscript{15}. This study represents a first methodological step towards adaptive resolution MD simulations also of systems of biological relevance, e.g., a protein in water.

The paper is organized as follows: In Sec. II the dual scale model of a polymer chain in a liquid is presented. The hybrid numerical scheme and computational details are given in Sec. III. The results and discussion are reported in Sec. IV, followed by a summary and outlook in Sec. V.

II. MULTISCALE MODEL

We study a single generic bead-spring polymer solvated in a molecular liquid, as illustrated in Fig. 1. Solvent molecules within a distance $r_0$ from the polymer’s center of mass are modeled with all atomistic details to properly describe the specific polymer-solvent interactions. For the description of the solvent farther away, where the high resolution is not required, we use a lower resolution. The solvent molecules then, depending on their distance to the polymer’s center of mass, automatically adapt their resolution on the fly.

The model solvent is a liquid of $n$ tetrahedral molecules, as introduced in Refs.\textsuperscript{14} and \textsuperscript{15}. The solvent molecules in the high resolution regime are composed of four equal atoms with mass $m_0$. Their size $\sigma$ is fixed via the repulsive Weeks-Chandler-Andersen potential

$$U_{\text{rep}}(r_{\text{iaj}B}) = \begin{cases} 4\varepsilon \left[ \left( \sigma/\sigma_{\text{iaj}} \right)^{12} - \left( \sigma/\sigma_{\text{iaj}} \right)^6 + \frac{1}{4} \right], & \sigma_{\text{iaj}} \leq 2^{1/6}\sigma, \\ 0, & \sigma_{\text{iaj}} > 2^{1/6}\sigma, \end{cases}$$

(1)

with the cutoff at $2^{1/6}\sigma$. $\sigma$ and $\varepsilon$ are the standard Lennard-Jones units for lengths and energy, respectively. $r_{\text{iaj}B}$ is the distance between the atom $i$ of the molecule $\alpha$ and the atom $j$ of the molecule $\beta$. The neighboring atoms in a given molecule $\alpha$ are connected by finite extensible nonlinear elastic bonds

$$U_{\text{bond}}(r_{\text{iaj}A}) = \begin{cases} -(1/2)k_b \sigma_{\text{iaj}}^2 \ln \left[ 1 - (r_{\text{iaj}}/R_0)^2 \right], & r_{\text{iaj}} \leq R_0, \\ \infty, & r_{\text{iaj}} > R_0, \end{cases}$$

(2)

with divergence length $R_0=1.5\sigma$ and stiffness $k=30\varepsilon/\sigma^2$, so that the average bond length is approximately $0.97\sigma$ for $k_BT=\varepsilon$, where $T$ is the temperature of the system and $k_B$ is Boltzmann’s constant. For the coarse-grained solvent model in the low resolution regime we use one-site spherical molecules interacting via an effective pair potential,\textsuperscript{15} which was derived such that the statistical properties, i.e., the center of mass radial distribution function and pressure, of the high resolution liquid are accurately reproduced. This is also needed for the present study, since the motion of the high resolution sphere should not be linked to strong rearrangements in the liquid. The high and low resolutions freely exchange molecules through a transition regime containing hybrid molecules (see Fig. 1), where the molecules with no extra equilibration adapt their resolution and change the number of DOFs accordingly.\textsuperscript{14-16}

The polymer is modeled as a standard bead-spring polymer chain.\textsuperscript{15} It contains $N$ monomers, which represent chemical repeat units, usually comprising several atoms. The interactions between monomers (beads) are defined using Eqs. (1) and (2) with the rescaled values $\sigma_{\text{iaj}}=1.8\sigma$, $R_{0\text{b}}=R_0\sigma_{\text{b}}/\sigma=1.5\sigma_{\text{b}}$, and $k_B=3k\sigma^2/\sigma_{\text{b}}^2$, such that the size of the polymer bead $\sigma_{\text{b}}$ is approximately the same as the size of the solvent molecule.\textsuperscript{15} The average bond length between beads is rescaled accordingly. The bead mass is also increased $m_{\text{b}}=5m_0$ to make them behave more like Brownian particles. Standard Lorentz-Berthelot mixing rules\textsuperscript{19} are used for the interaction between monomers and the “atoms” of the solvent molecules.

Note that for studying the polymer chain in the coarse-grained solvent, one would have to parametrize a new polymer model as well in order to arrive at the same overall conformational properties. The lengths down to which the models then produce the same properties are important when one wants to switch between levels of resolution. This was done for polymeric melts\textsuperscript{20} where coarse-grained trajectories...
were employed to generate long time atomistic trajectories for polycarbonate. This, however, is beyond the scope of the present paper.

III. NUMERICAL SCHEME AND COMPUTATIONAL DETAILS

To smoothly couple the regimes of high and low levels of detail of the description of the solvent molecules, we apply the recently introduced AdResS scheme. There the molecules can freely move between the regimes; they are in equilibrium with each other with no barrier in between. The transition is governed by a weighting function \( w(r) \in [0, 1] \) that interpolates the molecular interaction forces between the two regimes and assigns the identity of the solvent molecule. We resort here to the weighting function defined in Ref. 15, which interpolates the molecular interaction forces between the two regimes and assigns the identity of the solvent molecule.

We resort here to the weighting function defined in Ref. 15,

\[
W(r) = \begin{cases} 
1, & r_0 > r \geq 0 \\
0, & r \geq r_0 + d
\end{cases}
\]

where \( r_0 \) is the radius of the high resolution region and \( d \) the interface region width, cf. 1. The radius \( r_0 \) must be chosen sufficiently large so that the whole polymer always stays within the high resolution solvent regime. \( w(r) \) is defined in such a way that \( w=1 \) corresponds to the high resolution, \( w=0 \) to the low resolution, and values \( 0 < w < 1 \) to the transition regime. This leads to intermolecular force acting between centers of mass of solvent molecules \( \alpha \) and \( \beta \),

\[
F_{\alpha\beta} = w(|R_\alpha - R|)w(|R_\beta - R|)F_{\alpha\beta}^{ex} + \left[ 1 - w(|R_\alpha - R|)w(|R_\beta - R|) \right]F_{\alpha\beta}^{cg}.
\]  

where \( F_{\alpha\beta}^{ex} \) is the total intermolecular force acting between centers of mass of the solvent molecules \( \alpha \) and \( \beta \). \( F_{\alpha\beta}^{ex} \) is the sum of all pair atom interactions between explicit tetrahedral atoms of the solvent molecule \( \alpha \) and explicit tetrahedral atoms of the solvent molecule \( \beta \). \( F_{\alpha\beta}^{cg} \) is the effective pair force between the two solvent molecules, and \( R_\alpha, R_\beta \) and \( R \) are the centers of mass of the molecules \( \alpha, \beta \) and the polymer, respectively. Note that one has to interpolate the forces and not the interaction potentials in Eq. (4) if Newton’s third law is to be satisfied. To suppress the unphysical density and pressure fluctuations emerging as artifacts of the scheme given in Eq. (4) within the transition zone we employ an interface pressure correction. The latter involves a re-parametrization of the effective potential in the system composed of exclusively hybrid molecules with \( w=1/2 \). Each time a solvent molecule crosses a boundary between the different regimes it gains or looses on the fly (depending on whether it leaves or enters the coarse-grained region) its equilibrated rotational and vibrational DOFs while retaining its linear momentum. This change in resolution requires to supply or remove “latent heat” and thus must be employed together with a thermostat that couples locally to the particle motion. This is achieved by coupling the particle motion to the dissipative particle dynamics (DPD) thermostat. This bears the additional advantage of preserving momentum conservation and correct reproduction of hydrodynamics in our \( nVT \) MD simulations. Because of the sufficiently large so that the whole polymer always stays between centers of mass of solvent molecules}

The validity condition for our approach thus requires \( D_{\text{polymer}} \ll D_{\text{solvent}} \), where \( D_{\text{polymer}} \) and \( D_{\text{solvent}} \) are the corresponding diffusion constants. This condition is trivially fulfilled in polymeric solutions and thus also in our simulations (see the next section).

We conducted all MD simulations using the ESPRESSO package. We integrated Newton’s equations of motion by a standard velocity Verlet algorithm with a time step \( \Delta t = 0.005 \tau \) and coupled the motion of the particles to a DPD thermostat with the temperature set to \( T = \varepsilon/k_B \). The DPD friction constant \( \zeta = 0.5 \tau^{-1} \), where \( \tau = (\varepsilon/m_0\sigma^2)^{-1/2} \), and the DPD cutoff radius was set equal to the cutoff radius of the effective pair interaction between solvent molecules, i.e., \( 3.5\sigma \). The width of the transition regime is \( 2.5\sigma \). Periodic boundary conditions and the minimum image convention were employed. After equilibration, trajectories of 5000\( \tau \) were obtained, with configurations stored every 5\( \tau \). These production runs were performed with a 10\( \varepsilon/\sigma \) force capping to prevent possible force singularities that could emerge due to overlaps with the neighboring molecules when a given molecule enters the transition layer from the coarse-grained side. The temperature was calculated using the fractional analog of the equipartition theorem

\[
\langle K_\alpha \rangle = \frac{\alpha k_B T}{2},
\]

where \( \langle K_\alpha \rangle \) is the average kinetic energy per fractional quadratic DOF with the weight \( w(r) = \alpha \). Via Eq. (5) the temperature is also rigorously defined in the transition regime in which the vibrational and rotational DOFs are partially “switched on/off.” The molecular number density of the solvent is \( \rho = 0.175/\sigma^3 \), which corresponds to a typical high density Lennard-Jones liquid. We considered three different system sizes with corresponding cubic box sizes: \( L = 25.0\sigma, 30.6\sigma, 34.2\sigma \). The reduced Lennard-Jones units are used in the remainder of the paper.

IV. RESULTS AND DISCUSSION

To validate the AdResS approach for the present polymer-solvent system, we carried out the analysis of the structural and dynamic properties of a polymer chain in the hybrid multiscale solvent compared to the corresponding fully explicit system where all solvent molecules are modeled with a high level of detail, i.e., as tetrahedral molecules.

A. Statics of the polymer chain and solvent

First, we focus on the explicit (ex) systems where the solvent is modeled with the high resolution all over the simulation box. These results are considered as the reference to check how well AdResS produces the same physics as the all-atom MD simulation. The reference average thermodynamic properties of the corresponding ex systems (polymer + explicitly resolved solvent) are listed in Table I.
TABLE I. Thermodynamic properties of the fully explicit systems (ex) of different chain lengths $N$ and box sizes $L$: average total pressure $\langle p \rangle$, average total temperature of the system $\langle T \rangle$, average temperature of the polymer $\langle T_{\text{polymer}} \rangle$, and average temperature of the solvent $\langle T_{\text{solvant}} \rangle$.

<table>
<thead>
<tr>
<th>$N$</th>
<th>10</th>
<th>20</th>
<th>30</th>
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<tbody>
<tr>
<td>$L$</td>
<td>25.0</td>
<td>30.6</td>
<td>34.2</td>
</tr>
<tr>
<td>$\langle p \rangle$</td>
<td>2.01±0.04</td>
<td>2.01±0.03</td>
<td>2.02±0.01</td>
</tr>
<tr>
<td>$\langle T \rangle$</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
</tr>
<tr>
<td>$\langle T_{\text{polymer}} \rangle$</td>
<td>1.0±0.5</td>
<td>1.0±0.3</td>
<td>1.0±0.2</td>
</tr>
<tr>
<td>$\langle T_{\text{solvant}} \rangle$</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
</tr>
</tbody>
</table>

The static properties of the solvent are characterized by the solvent radial center of mass distribution function (RDF) depicted in Fig. 2(a). This distribution function is within the thickness of the lines the same for all systems studied, including the hybrid ones. This is to be expected from our previous studies and the fact that the polymer fraction of volume is very small compared to that of the solvent.

The statistical properties of polymers are conveniently described by a number of quantities, namely, the radius of gyration

$$\langle R_G^2 \rangle = \frac{1}{N} \sum_i \langle (\mathbf{r}_i - \mathbf{R})^2 \rangle,$$

(6)

where $\mathbf{r}_i$ is the position vector of the $i$th monomer and $\mathbf{R} = N^{-1} \sum \mathbf{r}_i$ is the polymer’s center of mass, the end-to-end distance

$$\langle R_E^2 \rangle = \langle (\mathbf{r}_N - \mathbf{r}_1)^2 \rangle,$$

(7)

and the hydrodynamic radius

$$\frac{1}{R_H^2} = \frac{1}{N^2} \sum_{i \neq j} \langle \frac{1}{r_{ij}} \rangle,$$

(8)

where $r_{ij} = |\mathbf{r}_i - \mathbf{r}_j|$.\textsuperscript{26}

$\langle R_G^2 \rangle$ and $\langle R_E^2 \rangle$ scale as

$$\langle R_G^2 \rangle \propto \langle R_E^2 \rangle \propto N^{2\nu},$$

(9)

with the number of monomers $N$, where $\nu=0.5$ in $\theta$ solvent and $\nu=0.588$ in good solvent conditions,\textsuperscript{127,28} with rather small finite size corrections, while the hydrodynamic radius is known to show significant deviations from asymptotic behavior up to very long chains.\textsuperscript{29}

The single-chain static structure factor $S(q)$

$$S(q) = \frac{1}{N} \sum_{ij} \exp(iq \cdot (\mathbf{r}_i - \mathbf{r}_j)),$$

(10)

probes the self-similar structure within the scaling regime and thus provides an accurate way to determine $\nu$. $S(q)$ scales as

$$S(q) \propto q^{-1/\nu} \rightarrow q^2S(q) \propto q^{2-1/\nu}$$

(11)

in the regime $R_G^{-1} \ll q \ll b^{-1}$, where $b$ is the typical bond length. By fitting a power law to the computed $q^2 S(q)$ plotted in Fig. 2(b) we obtained the values for $\nu$ reported in Table II. Table II summarizes the values of all quantities defined above, which characterize the static properties of the polymer chain. The calculations were performed for $N = 10, 20, 30$.

Another property, which directly reveals the fractal structure of the chains, is the correlation hole, which is shown in Fig. 2(c). It directly shows, to which distance from the center of mass of the chains, the solvent density is perturbed by the chain beads. For the later application of the hybrid scheme it is important to define the explicit solvent regime large enough in order to cover the correlation hole completely.

The values of $\nu$ actually differ slightly from the asymp-
TABLE II. Summary of some polymer (embedded in the explicitly resolved ex solvent) properties: number of polymer beads N, size of the simulation box L, average maximal distance of a monomer from the polymer’s center of mass (∆r\text{max}), radius of gyration R_G, end-to-end distance R_E, hydrodynamic radius R_H, the static exponent ν, the exponent 2/z, where z is the dynamic exponent, and the longest relaxation time τ calculated using data from Table VI. The error bar for the exponents ν and 2/z is roughly 10%.

<table>
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<th>N</th>
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<tbody>
<tr>
<td>L</td>
<td>25.0</td>
<td>30.6</td>
<td>34.2</td>
</tr>
<tr>
<td>(∆r\text{max})</td>
<td>4.2±0.8</td>
<td>5.7±1.0</td>
<td>8.1±1.4</td>
</tr>
<tr>
<td>R_G=(R_G)\text{1/2}</td>
<td>2.7±0.5</td>
<td>3.8±0.6</td>
<td>5.0±0.8</td>
</tr>
<tr>
<td>R_E=(R_E)\text{1/2}</td>
<td>6.7±2.0</td>
<td>8.6±3.0</td>
<td>12±3</td>
</tr>
<tr>
<td>R_H=(R_H)\text{1/2}</td>
<td>3.3±0.3</td>
<td>4.0±0.3</td>
<td>4.7±0.4</td>
</tr>
<tr>
<td>ν</td>
<td>0.63</td>
<td>0.54</td>
<td>0.57</td>
</tr>
<tr>
<td>2/z</td>
<td>0.59</td>
<td>0.71</td>
<td>0.67</td>
</tr>
<tr>
<td>τ=R_G^2/(6D)</td>
<td>152</td>
<td>481</td>
<td>1390</td>
</tr>
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</table>

rotical value for the good solvent due to the finite chain lengths. Nevertheless, the agreement improves with the increasing N, as expected.

Let us now turn our attention to the hybrid solvent studied by MD simulation using AdResS.

To assure that the polymer is surrounded only by the explicitly resolved molecules, we determine first the maximal monomer distance from the polymer’s center of mass, ∆r\text{max}, as shown in Fig. 3 for all chain lengths studied. As shown ∆r\text{max} always stays within the high resolution regime.

Because for N=30 ∆r\text{max} gets rather close to R_G, we checked the static polymer properties for that case again. In Fig. 4 we compare the all explicit simulation to the two hybrid simulation schemes (with (ex-cg) and without (ex-cg)) the pressure correction in the transition regime for the chain form factor and the correlation hole. The agreement is excellent, showing that the proposed scheme should at least be capable of properly reproducing the conformational statistics of the embedded polymer in solution.

This is first checked by comparing the average thermodynamic properties as given in Table III for the hybrid ex-cg and ex-cg, systems (polymer+hybrid solvent). While the temperatures are identical the pressure correction in the interface layer reduces the pressure slightly, so that the hybrid system now also there agrees quite well with the all explicit simulation. The agreement with the reference values from Table I is very good. This is in line with the general static properties of the polymers, which are given in Tables IV and V, and compare very well to the data from Table II.

From the presented results we can conclude that AdResS faithfully reproduces the reference statics obtained from the simulations with a polymer embedded in the explicitly resolved solvent.

B. Dynamics of the polymer chain and solvent

While the conformational properties of the polymer in solution are well understood and properly described by the

FIG. 3. (Color online) Time evolution of the maximal monomer distance from the polymer’s center of mass, ∆r\text{max}, for polymers with N=10 beads and the radius of the high resolution regime r_0=7.0 (red line), N=20 and r_0=11.0 (green line), and N=30 and r_0=12.0 (blue line).

FIG. 4. (a) The static structure factor of the polymer with N=30 in the Kratky representation for all three cases studied: the fully explicit, the AdResS scheme with and without the interface pressure correction. (b) The correlation hole for the same systems as in (a).

TABLE III. Thermodynamic properties of systems with the polymer solvated in the hybrid ex-cg solvent and the hybrid ex-cg, solvent: average total pressure ⟨p⟩, average total temperature of the system ⟨T⟩, average temperature of the polymer ⟨T\text{polymer}⟩, and average temperature of the solvent ⟨T\text{solvent}⟩. For the temperatures the results cannot be distinguished.

<table>
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</tr>
</thead>
<tbody>
<tr>
<td>L</td>
<td>25.0</td>
<td>30.6</td>
<td>34.2</td>
</tr>
<tr>
<td>⟨p⟩\text{ex-cg}</td>
<td>2.03±0.02</td>
<td>2.04±0.01</td>
<td>2.04±0.03</td>
</tr>
<tr>
<td>⟨p⟩\text{ex-cg}_{ic}</td>
<td>2.01±0.01</td>
<td>2.01±0.01</td>
<td>2.01±0.01</td>
</tr>
<tr>
<td>⟨T⟩</td>
<td>1.0±0.02</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
</tr>
<tr>
<td>⟨T\text{polymer}⟩</td>
<td>1.0±0.5</td>
<td>1.0±0.3</td>
<td>1.0±0.2</td>
</tr>
<tr>
<td>⟨T\text{solvent}⟩</td>
<td>1.0±0.02</td>
<td>1.0±0.01</td>
<td>1.0±0.01</td>
</tr>
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</table>
adaptive resolution approach, the situation for the dynamics is much less clear. By changing the DOFs not only the structure but also the dynamical properties are altered, however, in a way which is less understood. It is also not a priori clear, whether an approach, which produces a precise coarse graining for structural properties, does this for dynamical properties as well. In a recent study of small additive molecules to a polymer melt it was shown that while the length scaling is identical, the time scaling can be different.30 In the present situation the influence of the transition regime poses additional difficulties.

In order to determine the dynamical properties of the solvent and solute we calculated the respective diffusion coefficients. The diffusion coefficient of a species is computed from the center of mass displacements using the Einstein relation

$$D = \frac{1}{6} \lim_{t \to \infty} \frac{\langle |\mathbf{R}_i(t) - \mathbf{R}_i(0)|^2 \rangle}{t} = \frac{1}{6} \lim_{t \to \infty} \frac{\langle \Delta R^2 \rangle}{t},$$

where $\mathbf{R}_i(t)$ is the center of mass position of the molecule $i$ (which can be either a solvent or a solute molecule) at time $t$, and averaging is performed over all choices of time origin and, in the case of solvent, over all solvent molecules.

Figure 5 shows this for the solvent molecules’ centers of mass as a function of time for the different systems indicated. All the curves in Fig. 5, except the one for the coarse-grained solvent, coincide. Thus the effect of the polymer on the diffusivity of the solvent molecules is negligible. In other words, the dilution is strong enough that the polymer effect on the solvent dynamics is very small. However, the coarse-grained solvent molecules move faster than the explicit ones. This is a consequence of the reduced number of DOFs causing a time scale difference in the dynamics of the coarse-grained system.14,15 While this can be very advantageous in some cases, one can also adjust $D$ by an increased back-ground friction in the DPD thermostat.18,31 The diffusion coefficient $D$ of the solvent was obtained by fitting a linear function to the curves depicted in Fig. 5 and the obtained values are $D_{\text{bulk cg}} = 0.036$ and $D_{\text{bulk ex}} = 0.057$ for the explicit and coarse-grained solvent, respectively. The question to ask here is to what extent does this have any influence on the dynamics of the embedded polymer.

Within the Zimm model27 for polymer chain dynamics, which is known to describe the scaling of the dynamics in dilute solutions of polymers rather well and which takes into account the hydrodynamic interactions, the polymer diffusion coefficient scales as

$$D \propto N^{-\tau} \propto R_G^{-1} \propto R_G^{-1}.$$

The longest relaxation time $\tau = R_G^2/(6D)$, i.e., the Zimm time $\tau_{Z} \propto R_G^2 = R_G^2$, is the time the chain needs to move its own size. $z=3$ is the dynamic exponent. Note that the motion of inner monomers within the appropriate scaling regime should be independent of $N$. A scaling analysis immediately yields for the mean square displacement of a monomer $i$,

$$\langle \Delta R^2 \rangle = \langle |\mathbf{r}_i(t) - \mathbf{r}_i(0)|^2 \rangle \propto t^{2z} = t^{2/3}$$

for distances significantly larger than the bond length and smaller than $\langle R^2 \rangle$, i.e., times smaller than $\tau_Z$. For the center of mass of the chains a diffusive behavior for the mean square displacement $\langle \Delta R^2(t) \rangle$ is always observed. Although the chains are relatively short, at least for $N=30$ one expects a behavior relatively close to the above mentioned idealized scheme.29 Figure 6 shows $\langle \Delta R^2(t) \rangle$ and $\langle \Delta R^2(t) \rangle$ for polymer chains with $N=10,20,30$ embedded in the different solvent scenarios studied.

### Table IV

<table>
<thead>
<tr>
<th>$N$</th>
<th>10</th>
<th>20</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>$L$</td>
<td>25.0</td>
<td>30.6</td>
<td>34.2</td>
</tr>
<tr>
<td>$r_0$</td>
<td>7.0</td>
<td>11.0</td>
<td>12.0</td>
</tr>
<tr>
<td>$\langle \Delta r_{\text{max}} \rangle$</td>
<td>4.0±0.8</td>
<td>5.9±1.2</td>
<td>8.6±1.5</td>
</tr>
<tr>
<td>$R_G=(R_G)_{1/2}$</td>
<td>2.7±0.4</td>
<td>3.9±0.7</td>
<td>5.2±0.8</td>
</tr>
<tr>
<td>$R_E=(R_E)_{1/2}$</td>
<td>6.6±2.1</td>
<td>9.4±3.0</td>
<td>13.3±3.3</td>
</tr>
<tr>
<td>$R_H=(R_H)_{1/3}$</td>
<td>3.2±0.3</td>
<td>4.0±0.4</td>
<td>4.8±0.4</td>
</tr>
<tr>
<td>$\nu$</td>
<td>0.59</td>
<td>0.55</td>
<td>0.57</td>
</tr>
<tr>
<td>$2/z$</td>
<td>0.69</td>
<td>0.71</td>
<td>0.77</td>
</tr>
<tr>
<td>$\tau=R_G^2/(6D)$</td>
<td>152</td>
<td>362</td>
<td>1127</td>
</tr>
</tbody>
</table>

*TABLE IV. Summary of some polymer (embedded in the hybrid ex-cg solvent) properties: number of polymer beads $N$, size of the simulation box $L$, radius of the high resolution regime $r_0$, average maximal distance of a monomer from the polymer’s center of mass $\langle \Delta r_{\text{max}} \rangle$, radius of gyration $R_G$, end-to-end distance $R_E$, hydrodynamic radius $R_H$, the static exponent $\nu$, the exponent $2/z$, where $z$ is the dynamic exponent, and the longest relaxation time $\tau$ calculated using data from Table VI. The error bar for the exponents $\nu$ and $2/z$ is roughly 10%.*
In all cases the observed exponents for $\langle \Delta r^2(t) \rangle$ and $\langle \Delta R^2(t) \rangle$ are close to 0.7±0.05 and 1±0.05, respectively. Also the amplitudes of the displacements of the inner beads are almost the same for all chain lengths studied. This is in good agreement with earlier studies on different generic polymer models in an explicit solvent as well as studies of chains in a hybrid lattice Boltzmann solvent. While the ratio of the diffusion constants for different chain lengths roughly follow the expected scaling, even though it cannot hold precisely due to the different box sizes, we here observe a tendency to a weakly accelerated diffusion in the hybrid regime. This is most evident for the hybrid ex-cg case. Two different aspects might play a role here. First the viscosity in the coarse-grained outer regime is smaller, which must have an effect on the diffusion. Second, the small pressure and density fluctuations in the transition regime might contribute to the effect as well.

Although this is only a very first and incomplete test, it shows that within the AdResS scheme essential aspects of the dynamical properties of the embedded polymer chain are reasonably well reproduced.

V. SUMMARY AND OUTLOOK

In this paper we presented a hybrid multiscale MD simulation of a generic macromolecule in a solvent using the recently proposed AdResS method. The solvent surrounding the macromolecule is represented with a sufficiently high level of detail so that the specific interactions between the solvent and the solute are correctly taken into account. The solvent farther away from the macromolecule, where the high resolution is not needed, is represented on a coarse-grained level. The high and low resolution regimes freely exchange solvent molecules, which change their resolution accordingly. To correctly simulate momentum transport through the solvent, we use the DPD thermostat. The simulation results show that AdResS accurately reproduces the thermodynamic and structural properties of the system. The presented methodology is an extension of AdResS to simulations of a solvation cavity and represents a first step towards the treatment of more realistic systems such as biomacromolecules embedded in water. Work along these lines is already underway.

TABLE VI. Diffusion constant of the polymer chain embedded in three different solvents: explicitly resolved ex, hybrid ex-cg, and hybrid ex-cg_{ic}. Though the statistics of the data is rather poor we can estimate the error bar roughly to 10–15%. For comparison, the diffusion coefficients of the explicit and coarse-grained solvents are $D_{\text{bulk,ex}} = 0.036$, and $D_{\text{bulk,cg}} = 0.057$ respectively, with an effect of the polymers too small to determine here. Hence $D_{\text{polymer}} = D_{\text{solvent}}$.

<table>
<thead>
<tr>
<th>N</th>
<th>10</th>
<th>20</th>
<th>30</th>
</tr>
</thead>
<tbody>
<tr>
<td>D(ex)</td>
<td>0.008</td>
<td>0.005</td>
<td>0.003</td>
</tr>
<tr>
<td>D(ex-cg)</td>
<td>0.009</td>
<td>0.006</td>
<td>0.0045</td>
</tr>
<tr>
<td>D (ex-cg_{ic})</td>
<td>0.0085</td>
<td>0.006</td>
<td>0.0035</td>
</tr>
</tbody>
</table>

FIG. 6. Log-log plot of the time dependence of the mean square displacement of a single monomer (considered are only monomers near the chain’s center of mass) for polymers and their centers of mass with $N=$10,20,30 solvated in (a) the ex solvent, (b) the hybrid ex-cg solvent, and (c) the ex-cg_{ic} solvent as indicated.
ACKNOWLEDGMENTS

The authors thank Thomas Vettorel, Vagelis Harmandaris, Benedict Reynolds, and Burkhard Dünweg for useful discussions. This work is supported in part by the Volkswagen Foundation. One of the authors (M.P.) acknowledges the financial support from the state budget by the Slovenian Research Agency under Grant No. P1-0002.

1 P.-G. de Gennes, Scaling Concept in Polymer Physics (Cornell University, Ithaca, 1979).
25 http://www.espresso.mpg.de
26 Note that the definition of \( \chi \) given in Eq. (8) is only correct for an infinite simulation box. For a finite box we have to also consider the hydrodynamic interactions with the periodic images. The value of in such an infinite simulation box. For a finite box we have to also consider the hydrodynamic interactions with the periodic images. The value of \( \chi \) deviates from the value obtained using formula (8) (Refs. 8 and 29). However, since our aim in the present work is only to compare the properties of the polymer chain from the hybrid simulation with the corresponding ones from the all-atom simulation we here do not take the finite size correction into account and use formula (8) for the definition of \( \chi \).